

On Comparison of Experimental Thermochemical Data with G3 Theory

Larry A. Curtiss,^{*,†} Krishnan Raghavachari,[‡] Paul C. Redfern,[†] Gary S. Kedziora,[§] and John A. Pople[§]

Materials Science and Chemistry Divisions, Argonne National Laboratory, Argonne, Illinois 60439, Bell Laboratories, Lucent Technologies, Murray Hill, New Jersey 07974, and Department of Chemistry, Northwestern University, Evanston, Illinois 60208

Received: July 26, 2000; In Final Form: October 16, 2000

The results of assessments of methods for computing molecular thermochemical data can depend significantly on how comparison with experimental data is done. This is illustrated for two cases involving G3 theory: the energy of SiF₄ and the G2/97 test set.

In the past decade significant progress has been made in developing quantum chemical methods for accurately predicting molecular thermochemical data. An important part of the development of such quantum chemical methods is their critical assessment on test sets of accurate experimental data. We recently published a paper on the development of G3 theory¹ and its evaluation on the G2/97 test set.^{2,3} Since then two papers have appeared that give different interpretations of the accuracy of G3 theory. Martin and Taylor⁴ (MT) suggested that G3 theory has a “large error” for SiF₄, one of the molecules in the G2/97 test set, based on their theoretical calculations. This is in contradiction to our conclusions in ref 1. In another paper Montgomery et al.⁵ reanalyzed the accuracy of G3 theory on the G2/97 test set and found that it had a smaller mean absolute deviation from experiment (0.94 kcal/mol) compared to our published value in ref 1 (1.01 kcal/mol). These two differences in the interpretation of the accuracy of G3 theory need further explanation. In this note we discuss in more detail the G3 error in the energy of SiF₄ and our criteria for assessments on the G2/97 test set.

Martin and Taylor⁴ compared the G3 value of the atomization energy, ΣD_e , of SiF₄ (571.7 kcal/mol) with their “benchmark” value of 573.9 kcal/mol. They give the G3 error to be 2.2 kcal/mol compared to the benchmark value, and 4.1 if scalar relativistic corrections are included. They conclude that G3 exhibits a “large error” for SiF₄. The first point to be made about the analysis of MT is that they use their theoretical ΣD_e (SiF₄) to assess the G3 value. If G3 is strictly compared with experimental data, the conclusions are different. The directly measured experimental quantity for SiF₄ is its enthalpy of formation: $\Delta H_f^0(298\text{ K}) = -385.98 \pm 0.2$ kcal/mol⁶ or -386.18 ± 0.18 kcal/mol.⁷ The G3 enthalpy of formation at 298 K (-384.9 kcal/mol) differs by only 1.1 kcal/mol from the first experimental value,⁶ which is included in the G2/97 test set. The experimental atomization energy at 0 K, $\Sigma D_0(\text{SiF}_4)$, can be derived from the measured values for $\Delta H_f^0(298\text{ K})$ of SiF₄ [-385.98], $\Delta H_f^0(0\text{ K})$ of Si(g) [106.6 kcal/mol⁶], $\Delta H_f^0(0\text{ K})$ of F(g) [18.47 kcal/mol⁶] and the temperature corrections of these species [0.76 kcal/mol for Si(cr),⁶ 1.05 kcal/mol⁶ for F₂(g), and 3.67 kcal/mol⁴ for SiF₄]. The resulting

experimental ΣD_0 of 565.2 kcal/mol differs by only 1.1 kcal/mol from the G3 value of 564.1 kcal/mol. Finally, inclusion of the experimental zero-point energy (8.03 kcal/mol^{4,8}) gives a $\Sigma D_e(\text{SiF}_4)$ of 573.2 kcal/mol, which differs by 1.4 kcal/mol from the G3 value of 571.7 kcal/mol.⁹ Thus, G3 is quite accurate for SiF₄, based on the best available experiment data.

The second point to be noted about the MT results for G3 theory on SiF₄ is that it is incorrect to add a scalar relativistic correction to the G3 energies without re-optimizing the G3 higher level correction (HLC) parameter values. The overall mean absolute deviation for the G2/97 test set remains about the same when the HLC is re-optimized with relativistic corrections included.^{10,11} When this is done, the error in the SiF₄ enthalpy of formation increases from 1.1 kcal/mol to 2.3 kcal/mol (or 2.0 kcal/mol if the MT relativistic correction is used). This error is much less than what is obtained by MT without re-optimization.

Martin and Taylor⁴ have recommended a new value for the Si(g) atomic enthalpy of formation [107.2 ± 0.38 kcal/mol] that is based on their theoretical ΣD_e value and the experimental value for the ΔH_f^0 of SiF₄. If we use this value, it would increase the error in ΣD_0 and ΣD_e given by G3 theory by about 0.6 kcal/mol. We did not use the new value for the ΔH_f^0 of Si(g) in the analysis above for the following reason. The new ΔH_f^0 of Si(g) recommended by MT is obtained in part from the experimental ΔH_f^0 of SiF₄, the quantity that we are calculating. Thus, including it in our derivation would introduce circular reasoning that should be avoided (see below for more discussion of this point).

We now address the second subject of this note. Montgomery et al.⁵ reported that the mean absolute deviation of G3 theory is 0.94 kcal/mol for the G2/97 test set. In contrast we originally reported this mean absolute deviation as 1.01 kcal/mol for the G2/97 test set.^{1,12} There are two reasons for the difference between the two analyses of the accuracy of G3 theory. First, Montgomery et al. eliminate four entries in the statistical analysis of the G2/97 test set: the enthalpies of formation of CF₂O, C₂F₄, and CH₂CHCl, and the ionization potential of B₂F₄. They do this because there is theoretical evidence that the experimental values are in error. In our analysis we have chosen not to throw out experimental data unless there is new experimental evidence that warrants it. In only one case is there such evidence, CF₂O.² In the other cases there is no new experimental evidence to

[†] Argonne National Laboratory.

[‡] Lucent Technologies.

[§] Northwestern University.

support dropping the energies and, thus, we have not dropped them in our analysis. Second, Montgomery et al. have used “theoretical” atomic enthalpies of formation for Si⁴ and Be¹³ and experimental atomic enthalpies for all other elements in the calculation of molecular enthalpies of formation. We use experimental values for all elements, despite some uncertainty in the Si and Be values.¹⁴ The reason that we do not use these “theoretical” atomic enthalpies is that they are derived in part from an experimental molecular enthalpy that is part of the test set, which may bias the assessment process. If the two changes noted above are not included in this analysis of the G2/97 test set, the mean absolute deviation is 1.01 kcal/mol for G3 theory the same as we reported in ref 1.¹⁵ Thus, elimination of these items produces significant change.

The problem with using a “theoretical” value for an atomic enthalpy in assessments of thermochemical data is illustrated by the case of Si(g). The $\Delta H_f^0(0\text{ K})$ of Si(g) from the JANAF tables⁶ is 106.6 ± 1.9 kcal/mol. The uncertainty was revised to 1.0 kcal/mol by Desai.¹⁶ In 1992 Grev and Schafer suggested, on the basis of theoretical calculations combined with the experimental enthalpy of formation of SiH₄, a new value of 108.1 kcal/mol for the $\Delta H_f^0(0\text{ K})$ of Si(g). It was used by Montgomery et al.¹⁷ in an earlier assessment study. As discussed above, MT in 1999 recommended a value of 107.15 ± 0.38 kcal/mol⁴ based on “benchmark” calculations in combination with the experimental enthalpy of formation of SiF₄. This is the value used by Montgomery et al. in the assessment of G3 theory discussed here. In 1999 Dixon and Feller¹⁸ also reported “benchmark” calculations on SiF₄ and indicated that there was not enough evidence to challenge the experimental value of $\Delta H_f^0(0\text{ K})$ of Si. Thus, the published “benchmark” calculations on this subject are conflicting and further work is welcome.

Montgomery et al.⁵ assess their CBS-QB3 method on the G2/97 test set. The CBS-QB3 method is a modification of the CBS-Q method that is based on density functional geometries and zero-point energies. They have published two versions of this method, an earlier one based on localization using an extended basis set¹⁷ and the latest based on localization using a minimal basis set.⁵ Montgomery et al.⁵ give the mean absolute deviation from experiment of the latest CBS-QB3 method as 1.10 kcal/mol for the G2/97 test set using their analysis scheme. Using our criteria it increases to 1.16 kcal/mol. The original version^{17,19} of CBS-QB3 has a mean absolute deviation of 1.21 kcal/mol²⁰ for the G2/97 test set using our criteria. Thus, there is some overall improvement due to the change in the localization procedure (1.21 to 1.16 kcal/mol). Note that the two versions of CBS-QB3 give different molecular energies in some cases. For example, SO₂ differs by 0.6 kcal/mol, CCl₄ by 2.4 kcal/mol, and C₆H₆ by 0.6 kcal/mol.^{17,20}

In summary, we have shown that the results of assessments of methods for computing molecular thermochemical data can depend significantly on how comparison with experimental data is done. In all of our assessments^{1–3} including our most recent

on that presented the G3/99 test set²¹ we have avoided including any theoretical input in the experimental test set. If theoretical input is included in the experimental data, the resulting analysis may differ as shown by several examples in this note.

Acknowledgment. This work was supported at Argonne National Laboratory by the U.S. Department of Energy, Division of Materials Sciences, under contract No. W-31-109-ENG-38, and at Northwestern University by the National Science Foundation under Grant No. CHEM-89-18623.

References and Notes

- (1) Curtiss, L. A.; Raghavachari, K.; Redfern, P. C.; Rassolov, V.; Pople, J. A. *J. Chem. Phys.* **1998**, *109*, 7764.
- (2) Curtiss, L. A.; Raghavachari, K.; Redfern, P. C.; Pople, J. A. *J. Chem. Phys.* **1997**, *106*, 1063.
- (3) Curtiss, L. A.; Redfern, P. C.; Raghavachari, K.; Pople, J. A. *J. Chem. Phys.* **1998**, *109*, 42.
- (4) Martin, J. M. L.; Taylor, P. R. *J. Phys. Chem. A* **1999**, *103*, 4427.
- (5) Montgomery, J. A., Jr.; Frisch, M. J.; Ochterski, J. W.; Petersson, G. A. *J. Chem. Phys.* **2000**, *112*, 6532.
- (6) *NIST-JANAF Thermochemical Tables*, 4th ed.; Chase, M. W., Jr., Ed.; *J. Phys. Chem. Ref. Data* 1998, Monograph 9.
- (7) Johnson, G. K. *J. Chem. Thermodyn.* **1986**, *18*, 801.
- (8) McDowell, R. S.; Reisfeld, M. J.; Patterson, C. W.; Krohn, B. J.; Vasquez, M. C.; Laguna, G. A. *J. Chem. Phys.* **1982**, *77*, 4337.
- (9) It should be also noted that G3 theory it is not expected to be as accurate for D_e values as it is for ΔH_f^0 or ΣD_o values because its HLC parameters have been derived to give the best agreement with experiment for enthalpies of formation. The HLC takes into account not only deficiencies in the total energies, but also deficiencies in other quantities such as zero-point energies.
- (10) Kedziora, G. S.; Pople, J. A.; Rassolov, V.; Ratner, M. A.; Redfern, P. C.; Curtiss, L. A. *J. Chem. Phys.* **1999**, *110*, 7123.
- (11) Kedziora, G. S.; Pople, J. A.; Rassolov, V.; Ratner, M. A.; Redfern, P. C.; Curtiss, L. A., submitted.
- (12) Curtiss, L. A.; Raghavachari, K.; Redfern, P. C.; Pople, J. A. *J. Chem. Phys.* **2000**, *112*, 7374.
- (13) Ochterski, J. W.; Petersson, G. A.; Wiberg, K. B. *J. Am. Chem. Soc.* **1995**, *117*, 11299.
- (14) See ref 2 for details on the procedure used to calculate enthalpies of formation of molecules.
- (15) Montgomery et al.⁵ have also revised some of the experimental values with slightly different values. This has little overall effect on the results.
- (16) Desai, P. D. *J. Phys. Chem. Ref. Data* **1986**, *15*, 967.
- (17) Montgomery, J. A., Jr.; Frisch, M. J.; Ochterski, J. W.; Petersson, G. A. *J. Chem. Phys.* **1999**, *110*, 1.
- (18) Feller, D.; Dixon, D. A. *J. Phys. Chem.* **1999**, *A103*, 6413.
- (19) *Gaussian 98* (Revisions A.3); M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, V. G. Zakrzewski, J. A. Montgomery, R. E. Stratmann, J. C. Burant, S. Dapprich, J. M. Millam, A. D. Daniels, K. N. Kudin, M. C. Strain, O. Farkas, J. Tomasi, V. Barone, M. Cossi, R. Cammi, B. Mennucci, C. Pomelli, C. Adamo, S. Clifford, J. Ochterski, G. A. Petersson, P. Y. Ayala, Q. Cui, K. Morokuma, D. K. Malick, A. D. Rabuck, K. Raghavachari, J. B. Foresman, J. Cioslowski, J. V. Ortiz, B. B. Stefanov, G. Liu, A. Liashenko, P. Piskorz, I. Komaromi, R. Gomperts, R. L. Martin, D. J. Fox, T. Keith, M. A. Al-Laham, C. Y. Peng, A. Nanayakkara, C. Gonzalez, M. Challacombe, P. M. W. Gill, B. G. Johnson, W. Chen, M. W. Wong, J. L. Andres, M. Head-Gordon, E. S. Replogle, and J. A. Pople, Gaussian, Inc., Pittsburgh, PA, 1998.
- (20) Curtiss, L. A.; Redfern, P. C.; Frurip, D. J. *Reviews of Computational Chemistry*; Lipkowitz, K. B., Boyd, D. B., Eds.; Wiley-VCH: New York, 2000; Vol. 15, pp 147–202.